# **Bibliographic Analysis with the Citation Network Topic Model**

## HIGHLIGHT

**Background:** Applying topic models to bibliographic data is challenging due to the non-trivial combination of text and network modelling. Jointly modelling text and network with a full Bayesian model also leads to complicated learning algorithms which are not easy to implement.

**Objectives:** Propose a topic model for bibliographic data that

- 1. Jointly models text and network, as well as additional metadata (*e.g.* authors).
- 2. Gives a learning algorithm that is simple to implement and understand.
- 3. Provides comprehensive qualitative results for corpus exploration.

**Contributions:** Citation Network Topic Model

- 1. A full Bayesian non-parametric topic model for bibliographic data.
- 2. Models text with a hierarchical Pitman-Yor process (HPYP) topic model.
- 3. Models citations with a Poisson network model.
- 4. Gives a novel learning algorithm that marginalises out probability distributions, treating text and citation data as counts.
- 5. Outperforms previous work on model fitting and clustering.
- 6. Facilitates various qualitative analysis such as authors and topics analysis.



**Author Topics** 

#### **Characteristics:**

- 1. Authors' topics influence documents' topics.
- 2. Document topics hierarchy reflects the difference in text and citations. 3. Word burstiness is modelled following Buntine and Mishra (2014).

### Full model:

 $\mu \sim \operatorname{GEM}(\alpha^{\mu}, \beta^{\mu})$  $\nu_a | \mu \sim \text{PYP}(\alpha^{\nu_a}, \beta^{\nu_a}, \mu)$  $\theta'_d | a_d, \nu \sim \text{PYP}(\alpha^{\theta'_d}, \beta^{\theta'_d}, \nu_{a_d})$  $\theta_d | \theta'_d \sim \text{PYP}(\alpha^{\theta_d}, \beta^{\theta_d}, \theta'_d)$  $\gamma \sim \mathrm{PYP}(\alpha^{\gamma}, \beta^{\gamma}, H^{\gamma})$  $\phi_k | \gamma \sim \text{PYP}(\alpha^{\phi_k}, \beta^{\phi_k}, \gamma)$ 

 $\phi'_{dk} | \phi_k \sim \text{PYP}(\alpha^{\phi'_{dk}}, \beta^{\phi'_{dk}}, \phi_k)$  $z_{dn}|\theta_d \sim \text{Discrete}(\theta_d)$  $w_{dn}|z_{dn}, \phi'_d \sim \text{Discrete}(\phi'_{dz_{dn}})$  $x_{ij}|\lambda_{ij} \sim \text{Poisson}(\lambda_{ij})$ 



 $\lambda_{ij} = \lambda_i^+ \lambda_j^- \sum \lambda_k^T \theta_{ik}' \theta_{jk}'$ 

# **MODEL REPRESENTATION**

**Count representation:** Each probability vector ( $\nu, \theta$  etc.) is marginalised out and information is stored as counts. The probability vector, in Chinese Restaurant Process terminology, is represented by integers known as customer counts c and table counts t. Its explicit probability vector can be recovered from these counts.

**Modularised representation:** CNTM's posterior likelihood can be broken down into product of marginalised posterior of the individual probability vectors. The marginalised posterior of each probability vector only depends on their counts and hyperparameters.

#### **Modularised posterior:**

 $f(\mathcal{N}) = \frac{(\beta^{\mathcal{N}} | \alpha^{\mathcal{N}})_{T^{\mathcal{N}}}}{(\beta^{\mathcal{N}})_{C^{\mathcal{N}}}} \prod S^{c_k^{\mathcal{N}}}_{t_k^{\mathcal{N}}, \alpha^{\mathcal{N}}}$ 

### **Posterior for HPYP topic model:**

$$f(\mu)\left(\prod_{a=1}^{A} f(\nu_{a})\right)\left(\prod_{d=1}^{D} f(\theta_{d}') f(\theta_{d}) \prod_{k=1}^{K} f(\phi_{dk}')\right)\left(\prod_{k=1}^{K} f(\phi_{k})\right) f(\gamma)\left(\prod_{v} \left(\frac{1}{|\mathcal{V}|}\right)^{t_{v}^{\gamma}}\right)$$

**Posterior for Poisson network model:** 

$$p(\mathbf{X}|\lambda,\theta') = \left(\prod_{i} (\lambda_{i}^{+})^{g_{i}^{+}} (\lambda_{i}^{-})^{g_{i}^{-}}\right) \prod_{ij} \left(\sum_{k} \lambda_{k}^{T} \theta_{ik}' \theta_{jk}'\right)^{x_{ij}} \exp\left(-\sum_{ijk} \lambda_{i}^{+} \lambda_{j}^{-} \lambda_{k}^{T} \theta_{ik}' \theta_{jk}'\right)$$

# **INFERENCE TECHNIQUES**

#### **Collapsed Gibbs sampler for HPYP topic model:**

- 1. The algorithm is analogous to LDA's Gibbs sampler.
- 2. First decrements a word and its associated customer counts c and table counts t. 3. Then jointly samples both topic assignments z and the associated counts.

## **Metropolis-Hastings algorithm for Poisson network:**

- 1. Introduces an auxiliary variable to denote the citing topic that causes a citation. 2. Assumes there is only one citing topic for each citation (reasonable in practice). 3 This simplifies the posterior of the Poisson network.

$$p(\mathbf{X}, \mathbf{Y}|\lambda, \theta') \propto \prod_{i} (\lambda_{i}^{+})^{g_{i}^{+}} (\lambda_{i}^{-})^{g_{i}^{-}} \prod_{k} \left(\lambda_{k}^{T}\right)^{\frac{1}{2}\sum_{i} h_{ik}} \prod_{ik} \theta'_{ik}^{h_{ik}} \exp\left(-\sum_{ij} \lambda_{i}^{+} \lambda_{j}^{-} \lambda_{y_{ij}}^{T} \theta'_{iy_{ij}} \theta'_{jy_{ij}}\right)$$

- 4. Note the probability vector  $\theta'$  in the posterior can be marginalised out. 5. This contributes additional counts to the existing customer and table counts. 6. The MH algorithm is straight forward and is similar to the Gibbs sampler.
- 7. High acceptance probabilities.

#### **Hyperparameter sampling:**

- 1. Auxiliary variable sampler for PYP hyperparameters.
- 2. Gibbs sampler for the Poisson network hyperparameters.

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for 
$$\mathcal{N} \sim \mathrm{PYP}(\alpha^{\mathcal{N}}, \beta^{\mathcal{N}}, \mathcal{P})$$

Datasets	Publications	Citations	Authors	Vocabulary	Words/Doc	%Repeat
1. ML	139227	1105462	43643	8322	59.4	23.3
2. M10	10310	77222	6423	2956	57.8	24.3
3. AvS	18720	54601	11898	4770	58.9	17.0
4. AI	3312	4608	_	3703	31.8	_
5. Cora	2708	5429	_	1433	18.2	_
6. PubMed	19717	44335	_	4209	67.6	40.1

## **Quantitative evaluations:** See paper for goodness of fit and clustering results. **Qualitative analysis:**

#### . Topic exploration from a collection of publication data. (ML dataset)

Topic	
Reinforcement Learning	
Object Recognition	
Data Mining	$\min$
$\operatorname{SVM}$	ke
Speech Recognition	recogniti

#### 2. Analyse authors' interest from the author-topic distribution. (M10 dataset)

Author	Topic	
<ul><li>D. Aerts</li><li>Y. Bengio</li><li>C. Boutilier</li><li>S. Thrun</li><li>M. Baker</li></ul>	Quantum Theory Neural Network Decision Making Robot Learning Financial Market	qua net

#### 3. Visualise author-topics relationships. (ML dataset)



DATA

**Research publications:** 3 corpus queried from CiteSeer<sup>X</sup> and 3 existing corpus.

## RESULTS

Top Words

reinforcement, agents, control, state, task

face, video, object, motion, tracking ining, data mining, research, patterns, knowledge ernel, support vector, training, clustering, space

tion, speech, speech recognition, audio, hidden markov

Top Words antum, theory, quantum mechanics, classical, quantum field tworks, learning, recurrent neural, neural networks, models decision making, agents, decision, theory, agent robot, robots, control, autonomous, learning market, risk, firms, returns, financial